## Strömungstechnik

Jan Philipp Heners

A Lanczos-filtered Harmonic Balance Method for Aeroelastic Applications of Turbomachinery Resolving Unsteady Turbulence Effects





# A Lanczos-filtered Harmonic Balance Method for Aeroelastic Applications of Turbomachinery Resolving Unsteady Turbulence Effects

Von der Fakultät Energie-, Verfahrens- und Biotechnik der Universität Stuttgart zur Erlangung der Würde eines Doktors der Ingenieurwissenschaften (Dr.-Ing.) genehmigte Abhandlung

> vorgelegt von Jan Philipp Heners aus Achern

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Tag der mündlichen Prüfung: 04.07.2022

Institut für Thermische Strömungsmaschinen und Maschinenlaboratorium der Universität Stuttgart

#### Berichte aus der Strömungstechnik

#### Jan Philipp Heners

## A Lanczos-filtered Harmonic Balance Method for Aeroelastic Applications of Turbomachinery Resolving Unsteady Turbulence Effects

D 93 (Diss. Universität Stuttgart)

Shaker Verlag Düren 2022

#### Bibliographic information published by the Deutsche Nationalbibliothek

The Deutsche Nationalbibliothek lists this publication in the Deutsche Nationalbibliografie; detailed bibliographic data are available in the Internet at http://dnb.d-nb.de.

Zugl.: Stuttgart, Univ., Diss., 2022

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Printed in Germany.

ISBN 978-3-8440-8828-1 ISSN 0945-2230

Shaker Verlag GmbH • Am Langen Graben 15a • 52353 Düren Phone: 0049/2421/99011-0 • Telefax: 0049/2421/99011-9

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#### **DECLARATION OF AUTHORSHIP**

I declare that this research effort has been composed by myself and that the work has not been submitted for any other degree or professional qualification. I confirm that the work submitted is my own. The contribution of other authors to this work has been explicitly indicated below. I confirm that appropriate credit has been given within this thesis where reference has been made to the work of others.

The work presented in Sections 2.3, 2.4 and 5.1 was previously presented at the 15th International Symposium on Unsteady Aerodynamics, Aeroacoustics and Aeroelasticity of Turbomachines (ISUAAAT 15) and published in the ASME Journal of Turbomachinery as "Investigation of the Impact of Unsteady Turbulence Effects on the Aeroelastic Analysis of a Low-Pressure Turbine Rotor Blade" by Jan Ph. Heners (the author), Prof. Dr. Damian Vogt (1st supervisor), Dr. Christian Frey, and Dr. Graham Ashcroft. It has therefore been subject to the independent review process of the ASME Journal of Turbomachinery.

The work presented in Chapter 3 was previously published in the Proceedings of the ASME Turbo Expo 2020 as "Prediction of the Unsteady Transition Behavior in Low Pressure Turbine Flows Using Time and Frequency Domain Methods" by Jan Ph. Heners (the author), Dr. Christoph Müller-Schindewolffs, Prof.

**Dr. Damian Vogt** (1st supervisor), and Frederik Blum. It has therefore been subject to the independent review process of the ASME Turbo Expo.

The work presented in Chapter 4 was previously published in the Proceedings of the 14th European Conference on Turbomachinery Fluid Dynamics & Thermodynamics (ETC 14). In addition to that, an extended version of the conference paper was published in the International Journal of Turbomachinery, Propulsion and Power. Both were published under the title "Prediction of Transient Pressure Fluctuations within a Low Pressure Turbine Cascade Using a Lanczos-Filtered Harmonic Balance Method" by Jan Ph. Heners (the author), Dr. Stephan Stotz, Annette Krosse, Detlef Korte, Maximilian Beck, and Prof. Dr. Damian Vogt (1st supervisor) and have therefore been subject to the independent review process of the European Turbomachinery Society.

The work presented in Setions 6.3 and 6.4 was previously presented at the ASME Turbo Expo 2022 and published in the ASME Journal of Turbo-machinery under the title "Evaluating the Aerodynamic Damping at Shock Wave Boundary Layer Interacting Flow Conditions with Harmonic Balance" by Jan Ph. Heners (the author), Dr. Christian Frey, and Dr. Björn Grüber. It has therefore been subject to the independent review process of the ASME Turbo Expo and the ASME Journal of Turbomachinery.

Stuttgart, 2021-10-01

#### **ABSTRACT**

This research thesis discusses the impact of unsteady turbulence effects on the numerical prediction of aerodynamic excitation mechanisms in turbomachinery flows. The limitations of existing solver structures based on a formulation in the frequency domain - the Harmonic Balance method, that is - promises to consider turbulence in an unsteady framework. Existing limitations to this are assessed and a solution approach to alleviate the identified sources of numerical instabilities is identified by the application of a Lanczos-type filter method.

After proper implementation and validation, the Harmonic Balance method enhanced by the filtering is used to evaluate the impact of unsteady turbulence on design tasks of aeroelastic interest. These are given by the prediction of the aerodynamic excitation and the aerodynamic damping, respectively. The impact of unsteady turbulence is investigated and quantified for both subsonic and transonic flow conditions. The evaluation of its quality and quantity is used to assess numerical solution approaches differing in the degree of exploited model order reduction. The assessed methods suffer from an increasing loss of information though benefit from lower requirements with regard to computational effort and run time.

#### ZUSAMMENFASSUNG

Die vorgelegte Promotionsschrift behandelt die Fragestellung des Einflusses instationärer Turbulenzeffekte auf die Vorhersage der aerodynamischen Anregung von Turbinen- und Verdichterkomponenten. Im Speziellen werden im Zuge der Arbeit zunächst die Ursachen für zu Beginn der Arbeit festgestellte Instabilitäten bei Anwendung des betrachteten numerischen Lösungsverfahren im Frequenzbereich identifiziert und durch Implementierung einer geeigneten Filtermethodik im Quellcode behoben.

Die Anwendung des stabilisierten Lösungsverfahrens in Verbindung mit einer entsprechenden Validierung erlaubt im Anschluss eine Bewertung des Einflusses der genannten instationären Turbulenzeffekte auf die in aeromechanischer Hinsicht relevanten Auslegungsaufgaben der Vorhersage von aerodynamischer Zwangserregung und Dämpfung. Dies wird sowohl für sub-, als auch für transsonische Strömungszustände untersucht und bewertet. Die Bewertung des Einflusses instationärer Turbulenzeffekte in Hinsicht auf Qualität und Quantität wird zur Analyse verschiedener numerischer Lösungsansätze verwendet, die aufgrund eines steigenden Grades von Modell-Ordnungs-Reduktion zunehmend unter Verlust an Information leiden, jedoch durch sinkende Anforderungen an die erforderliche Rechenleistung und Laufzeit profitieren.

#### **ACKNOWLEDGEMENTS**

This research thesis is a result of my work at MTU Aero Engines AG in Munich, Germany. During my research work in the Aerodynamics Department, I found considerable freedom to realise my ideas as well as an environment providing valuable insight in ongoing research and design issues concerning current and future generations of aircraft engines. Without the continuous support and exchange of the entire department, this research would never have achieved the presented level of industrial relevance and impact. Therefore, I would like to express my deepest gratitude to MTU Aero Engines AG and the Aerodynamics Department in particular for giving me the opportunity to realise this research effort.

I also want to express sincere thanks to my research advisor, Prof. Dr. tekn. Damian Vogt for guiding and supervising the presented work. At crucial stages of this research, he supported this effort by pointing out the achievements and, when necessary, hinting on an insufficient state of verification.

As the academic aspect of this work was assured by my supervisor Prof. Vogt from the University of Stuttgart, the same holds for Detlef Korte from MTU Aero Engines AG for what concerns the needs faced in an industrial context. The industrial value of this work as well as its contribution to the community of aeroelasticity in general is dedicated to him as to our continuous and detailed discussions.

A large part of the credit goes to the Numerical Methods Department of the Institute of Jet Propulsion at the German Aerospace Center DLR in Cologne. At DLR Cologne, I found a team that always supported me with their interest in my work, stimulating discussions and, if necessary, the expression of concerns about the progress of my research. In particular, I want to thank Dr. Christian Frey whose impact on this work can not be emphasised enough. Without his guidance, this work would have been lost. The same holds - maybe even without his further notice - for Dr. Jan Backhaus whose comments on this work at an early stage turned out to become a real game changer.

Furthermore, I want to thank a few people who supported this work in a way that must not be forgotten. First, I want to thank the students who accompanied me on my way to this thesis. These are Patrick Shoemaker from NUMECA Ingenieurbüro, Germany, Frederik Blum from Wieland Group, Germany, Nick Wildemans from TU Delft, The Netherlands, and Carlos Hünteler from TU München, Germany. The work and exchange with our students is and will be the main driver for our research.

Even more important than the students are, obviously, the teachers. The teachers who affected me and my research the most are Dr. Anne Gerdes from intersoft AG, Germany and Dr. Lars Radtke from TU Hamburg, Germany. Their patience, tuition and the way to share their knowledge expresses itself in the way I work, think and address problems to the present day.

Finally, every seized opportunity needs a person granting the required trust in the first place. Therefore, I want to close with my final thank to Dr. Karl Engel from MTU Aero Engines AG, Germany, for a lot but the most for giving me the possibility to proof my talent in a field of research I was allowed to enter without any experience.

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#### Nomenclature

ATF Altitude Test Facility

ATRD Advanced Turbine Research Demonstrator

BPF Blade Passing Frequency

CFD Computational Fluid Dynamics

CPU Central Processing Unit

CPUh CPU hour

DC Direct Current, Time-Invariant Component of a Fourier Series

DLR German Aerospace Center
DFT Discrete Fourier Transform

EO Engine Order

FFT Fast Fourier Transform HB Harmonic Balance

HPC High Pressure Compressor

HS Harmonic Set

IBPA Inter Blade Phase Angle

iDFT Inverse Discrete Fourier Transform

iFT Inverse Fourier TransformLPT Low Pressure Turbine

LE Leading Edge

MUSCL Monotonic Upwind Scheme for Conservation Laws

ND Nodal Diameter

NSV	Non-Synchronous Vibration	
PS	Pressure Side	
Q3D	Quasi Three-Dimensional Solution Approach	
RANS	Reynolds-averaged Navier Stokes Equations	
SS	Suction Side	
SWBLI	Shock Wave Boundary Layer Interaction	
TE	Trailing Edge	
TRACE	CFD Solver developed at DLR Cologne, Germany	
URANS	Unsteady Reynolds-averaged Navier Stokes Equations	
VPF	Vane Passing Frequency	
WG	Wake Generator	
WGPF	Wake Generator Passing Frequency	
С	Set of Primal Navier-Stokes Quantities	[-]
CFL	Courant-Friedrich-Lewy number	[-]
d	Set of Quantities required for Turbulence Modeling	[-]
δ	Boundary Layer Thickness	[m]
${\delta}_1$	Boundary Layer Displacement Thickness	[m]
$\Delta\eta_{\scriptscriptstyle  ext{is,Stage2}}$	Deviation of Isentropic Efficiency	[%]
$\mathcal{D}$	Alternative Definition of a Differential Operator	[-]
E	Specific Total Energy of a Fluid	$\left[\frac{m^2}{s^2}\right]$
f	Fundamental or Base Frequency of a Flow Field	[Hz
$f_{g}$	Specific, Local Generalised Force	$\left[\frac{N}{m^2}\right]$
$F_g$	Generalised Force	[N]
$\Phi$	Turbomachinery Flow Coefficient	[-]
$g_m$	Skewness within a Measured Data Set	[-]
$H_{12}$	Boundary Layer Shape Factor	[-]
γ	Intermittency of a Transitional Boundary Layer	[-]
$\gamma_{\delta}^*$	Intermittency averaged over the Boundary Layer	[-]
$rac{{m{\gamma}}_{m{\delta}}^{*}}{\widehat{I}}$	Equation System of the Discretised Flow Problem	[-]
k	Turbulence Kinetic Energy	$\left[\frac{m^2}{s^2}\right]$
$l_U$	Turbulence Length Scale	[m]
$l_{\rm ax}$	Axial Chord Length	[m]
m	Harmonic Index of the HB Method	[-]

M	Truncation Order of the HB Method	[-]
Ma	Mach Number	[-]
$Ma_{v_{2,in}}$	Mach Number at First Stator Exit Plane	[-]
$\mu$	Dynamic Viscosity of a Fluid	[Pa·s]
$\mu_t$	Eddy Viscosity of a Fluid	[Pa·s]
$\mu_2$	Second Central Moment or Variance of Data Set	$[V^2]$
$\mu_3$	Third Central Moment	$[V^3]$
N	Number of Sampling Points	[-]
$p_{t}$	Fluid Stagnation Pressure	[Pa]
q	Set of All considered URANS Quantities	[-]
ho	Fluid Density	$\left[\frac{\mathrm{kg}}{\mathrm{m}^3}\right]$
ho E	Total Energy of a Fluid	[J]
$\rho u$	Fluid Momentum	[N·s]
$\Pi_{\mathrm{tot}}$	Overall Total Pressure Ratio	[-]
$\Psi_t$	Eddy Viscosity Ratio	[-]
$\widehat{R}$	Non-Linear URANS Residual in the Frequency Domain	[-]
$R_N^*$	Non-Linear URANS Residual at Sampling Point N	[-]
$Re_{v_{2,in}}$	Reynolds number at the Second Stator Inlet Plane	[-]
$\text{Re}_{\Theta_t}$	Transition Reynolds Number	[-]
Sr	Strouhal Number	[-]
$\sigma$	Standard Deviation of a Data Set	[V]
$\sigma_{\it m}$	Lanczos- $\sigma$ Factor	[-]
t	Physical Time	[s]
T	Period of one Blade/Vane Passing	[s]
$T_{\scriptscriptstyle  m t}$	Total Temperature of a Fluid	[K]
$T_U$	Turbulence Intensity	[-]
$\Theta$	Amplitude Modulation	[-]
au	Pseudo Time	[-]
$ au_w$	Wall Shear Stress	[Pa]
$\theta$	Boundary Layer Momentum Thickness	[m]
и	Fluid Velocity	$\left[\frac{m}{s}\right]$
$\omega$	Turbulence Dissipation Rate	$[s^{-1}]$
$\Omega$	Angular Frequency	$[s^{-1}]$
$\mathcal{O}_M$	Truncation Error of a Fourier Series Expansion	[-]
Y	Axial Flow Direction	[m]