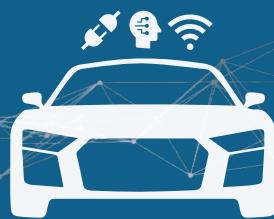


apl. Prof. Dr.-Ing. Daniel Görges (Hrsg.)

Xiaohai Lin

**Robust and Stochastic Model  
Predictive Control of Linear  
Systems with Predictable  
Additive Disturbance**

with Application to Multi-Objective  
Adaptive Cruise Control



# Robust and Stochastic Model Predictive Control of Linear Systems with Predictable Additive Disturbance

with Application to Multi-Objective Adaptive Cruise Control

## Robuste und stochastische modellprädiktive Regelung für lineare Systeme mit vorhersagbaren additiven Störungen

mit Anwendung für die multikriterielle adaptive Geschwindigkeitsregelung

Vom Fachbereich Elektrotechnik und Informationstechnik  
der Technischen Universität Kaiserslautern  
zur Verleihung des akademischen Grades  
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*Leonberg, April 2020*

*Xiaohai Lin*



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