

Mohamed Bouhaj

Experimental identification of SEA parameters for complex aircraft structures

Band 30



**Institut für
Modellierung und
Berechnung**

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Mohamed Bouhaj

Abstract

The Statistical Energy Analysis (SEA) is a widely used tool for the vibro-acoustic analysis of dynamical systems in the high frequency regime. In the application of SEA to complex assembled structures, a purely predictive model often exhibits errors, which are mainly due to a lack of accurate modelling of the power transmitted between subsystems and the power dissipated by each of them. The description of the power terms and the SEA equations depend essentially on two key parameters: The coupling loss factor (CLF) and the damping loss factor (DLF).

This thesis is included in the framework of Experimental SEA (ESEA) and aims at providing reliable input parameters to an SEA representation of complex systems, as well as procedures that allow a statistical description of these parameters.

A new stochastic energy model (SEM) is adopted to enhance the estimation of structural loss factors and assess their sensitivity to subsystems energy variance. For this purpose, expressions are obtained to randomly perturb the energy matrix elements and generate individual samples for the Monte Carlo (MC) technique applied to derive the ensemble averaged CLF. The method is firstly applied to an academic example of two rigid coupled plates, then to a more complex aircraft fuselage section. The results indicate that the SEM approach has the potential to significantly enhance the CLF estimate compared to classical matrix inversion methods. Moreover, the new derived sensitivity criterion gives the opportunity to guide the selection of SEA subsystems.

A complementary topic of this dissertation concerns the experimental determination of the damping loss factor of single isotropic plates, built-up aircraft structures and trim panels using the power injection method and the decay rate technique. The significance of the radiation loss and its impact on the derived DLF of the cabin components is addressed. The installation effect on estimated damping is elaborated by comparing measured levels in the semi-anechoic room with freely suspended cabin panels and in the aircraft with fully installed components. Finally, some conclusions are drawn about the frequency ranges, in which the respective procedures can be used.

keywords: Statistical Energy Analysis (SEA), experimental SEA, noise, vibro-acoustics, coupling loss factor, damping loss factor, power injection method, uncertainty, Monte Carlo (MC) method

Zusammenfassung

Die statistische Energieanalyse (SEA) ist eine weit verbreitete Methode für die Vorher sage von Lärm- und Vibrationspegeln im mittleren und hohen Frequenzbereich. Bei der SEA wird die Gesamtstruktur in schwach gekoppelte Substrukturen unterteilt. Die Beschreibung des Energietransfers zwischen den Subsystemen ist abhängig von den jeweiligen Kopplungsverlustfaktoren. Der Grad der Dissipationsenergie der Subsysteme wird durch Dämpfungsverlustfaktoren angegeben. Diese Faktoren bilden zusammen mit der modalen Dichte die wichtigsten SEA Parameter.

Validierte SEA Modelle von komplexen Systemen erfordern sowohl eine genaue Modellierung der Energietransmission zwischen den gekoppelten Subsystemen, als auch der dissipierten Leistungen. Daher liegt die größte Herausforderung der SEA in der Bestimmung der zuvor erwähnten Verlustfaktoren und der damit verbundenen Parameterunsicherheiten.

Die vorliegende Arbeit gibt einen Überblick über die vorhandenen Ansätze zur experimentellen Bestimmung der SEA Parameter und untersucht die Verfahrensgrenzen insbesondere bei der Anwendung in komplexen Flugzeugstrukturen. Basis dafür bildet die Power Injection Method (PIM), die es ermöglicht den Energiefluss zwischen gekoppelten Subsystemen abzuleiten und die SEA Parameter durch Invertieren der gemessenen Energiematrix zu identifizieren.

Eine weitere Herausforderung betrifft die Unsicherheit der in der experimentellen SEA involvierten Parameter. Mit dem neuen stochastischen Energiemodell (SEM) sind Prozeduren aufgezeigt, die eine stochastische Analyse der gemessenen Eingangsgrößen (wie Eingangsleistung und Vibrationsenergien) und der abgeschätzten Ausgangsgrößen (wie Verlustfaktoren) erlauben. Experimentelle Untersuchungen an akademischen und Flugzeugstrukturen zeigen zudem die Anwendbarkeit des entwickelten Ansatzes mit realen Testdaten. Die Ergebnisse zeigen, dass das neue Modell zu einer robusten Abschätzung der SEA Parameter führt, und gibt dem Anwender die Möglichkeit geeignete SEA-Subsysteme zu definieren.

Ein weiteres Augenmerk dieser Arbeit ist auf die Bestimmung der Dämpfungsver lustfaktoren von isotropen Platten und Flugzeugstrukturen durch den Einsatz ver schiedener experimentelle Verfahren gerichtet. Dabei gibt die Analyse Rückschlüsse auf das Dämpfungsverhalten der Kabinenbauteile, und ermöglicht sowohl den Einfluss der Einbaubedingungen zu untersuchen als auch Frequenzbereiche zu identifizieren, in welchen die jeweiligen Verfahren angewendet werden können.

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Nomenclature

Latin nomenclature

| | |
|---------------------------|---|
| $[a, b]$ | Interval with lower and upper bounds a, b |
| A | Matrix/vector (bold type) |
| c_0 | Speed of sound |
| D_{dir}^i | Direct field dynamic stiffness of the statistical subsystems |
| D_d | Dynamic stiffness of the deterministic subsystems |
| D_{tot} | Total dynamic stiffness of the system |
| $\langle E_i \rangle$ | Spatial averaged vibration energy of subsystem i |
| \hat{E} | Energy of single sensors |
| $E[X]$ | Expected value |
| E_{ij} | Energy level of subsystem i when exciting subsystem j |
| E_{ij}^n | Normalized energy levels |
| E | Vector of energy levels |
| f_{rev}^i | Vector of blocked forces on the deterministic interfaces due to the reverberant field |
| $f(x)$ | Probability density function |
| f_c | Coincidence frequency |
| H_{af} | Frequency response function acceleration/force |
| h_{ij} | Hybrid CLF |
| I | Identity matrix |
| [K] | Stiffness Matrix |
| L | SEA loss factor matrix |
| [M] | Mass Matrix |
| M | Mass |
| n | Sample size |
| N | Number of subsystems |
| n_i | Modal density |
| \widehat{P}_{in} | Power input at single locations |

Nomenclature

| | |
|---------------------------------------|--|
| $P_{i,\text{diss}}$ | Dissipated power in subsystem i |
| $P_{i,\text{in}}$ | Power input of subsystem i |
| P_{ij} | Net energy flow from subsystem i to subsystem j |
| P_{rad} | Radiated sound power |
| $\mathbf{S}_{\text{ff}}^{\text{ext}}$ | Cross-spectral density matrix of the external forces |
| s | Sample variance |
| S_{af} | Cross spectral density of the force and acceleration |
| $S_{i,\text{aa}}$ | Auto spectral density of the acceleration |
| T_R | Reverberation time |
| TL | Transmission loss |
| u_i | MC output variables |
| $\text{Var}[X]$ | Variance of a random variable X |
| v | Vibration velocity |
| \bar{x} | Arithmetic mean of x |
| $\bar{\bar{x}}$ | Arithmetic mean of x |
| X | Random variable |
| Y_{ii} | Input mobility |
| Y_{ii} | Transfer mobility |
| Z_i | Semi-infinite input impedance |

Greek nomenclature

| | |
|----------------------|---|
| η | Damping loss factor |
| η_b | Loss factor expressing damping at the boundaries of a subsystem |
| η_{ij} | Coupling loss factor between subsystem i and subsystem j |
| $\eta_i = \eta_{ii}$ | Internal loss factor |
| η_{rad} | Acoustic radiation loss factor |
| η_s | Structural loss factor |
| $[\eta^t]$ | Total loss factor matrix |
| σ | Radiation efficiency of the structure |
| Δf | Frequency bandwidth |
| ω | Center frequency |
| φ | Incidence angle |
| ρ_0 | Air density |

| | |
|-------------|---|
| μ | Expected mean value, or population mean |
| ν | Degree of freedom parameter |
| $\sigma(X)$ | Standard deviation |
| τ_{ij} | Transmission coefficient |
| ξ_i | MC input variables, random numbers |

List of indices

| | |
|-------------------------|---|
| $\langle \dots \rangle$ | Operator expressing spatial averaging |
| i | Index referring to the considered subsystem |
| j | Index referring to the excited subsystem |
| k | Index referring to an individual sensor |
| l | Index referring to an excitation location |
| Im(...) | Imaginary part operator |
| Re(...) | Real part operator |

General abbreviations

| | |
|------|--|
| A/C | Aircraft |
| BC | Boundary condition |
| BEM | Boundary Element Method |
| CB | Crossbeam |
| CI | Confidence Interval |
| CLF | Coupling Loss Factor |
| DLF | Damping Loss Factor |
| DRM | Decay Rate Method |
| ESEA | Experimental Statistic Energy Analysis |
| FEM | Finite Element Method |
| FP | Floor panel |
| FRF | Frequency response function |
| HPB | Half-Power Bandwidth |
| LSQI | Least Squares Minimization |
| MC | Monte Carlo |
| OHSC | Overhead stowage compartment |
| PDF | probability density function |

Nomenclature

| | |
|------|------------------------------|
| PIM | Power Injection Method |
| RT | Reverberation time |
| SEA | Statistic Energy Analysis |
| SEM | Stochastic Energy Model |
| SNR | Signal Noise Ratio |
| SR | Seat rail |
| SS | Subsystem |
| SVD | Singular value decomposition |
| SWP | Sidewall panel |
| VSEA | Virtual SEA |