IMPROVED DESIGN METHODS FOR THE BEARING CAPACITY OF FOUNDATION PILES



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by

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Abstract

Pile foundations are often used for civil structures, both offshore and onshore, which are placed on soft soils. Nowadays, there are many different methods used for the prediction of the pile bearing capacity. However, the resulting design values are often different from the values measured at pile load field tests. A reason for this is that there are many pile installation effects and (unknown) soil conditions which influence the pile bearing capacity. Another problem is that for many pile load field tests in the past, the residual stresses at the pile after pile installation, have been ignored unfortunately. This ignoring leads to a measured tip bearing resistance which is lower than the real tip bearing resistance (capacity), and a measured pile shaft friction which is higher than the real pile shaft friction.

The main aim of this thesis is, to come to a better understanding of the pile performance and especially the pile bearing capacity. In order to achieve this aim, many numerical loading simulations were computed for small displacements with the Finite Element Model Plaxis and many existing pile design methods have been studied. The pile installation process itself was modelled and simulated with the help of the material point method, MPM, which is able to handle large displacement numerical simulations. The used version of this MPM method was recently developed at the research institute Deltares in the Netherlands.

The results from the MPM simulations showed that there is a big difference between the bearing capacity of a pre-installed pile (no installation effect are taken into account) and the bearing capacity of a pile where the installations effects are taken into account. This proves in a numerical way the importance of the pile installation effects on the pile bearing capacity. However, the MPM numerical simulations were done only for jacked piles. Therefore, impact piles, vibrated piles etc., were not simulated. For this reason, there is not a detailed numerical study for the effect of each installation method specific on the pile bearing capacity. The fact that the installation effects, in general, has an important influence on the pile bearing capacity was already proven by field tests and centrifuge tests, and has been published before by several authors.

The performed numerical simulations show that during the loading and failure of a pile, a balloon shaped plastic zone develops around the pile tip, which is in fact the failure mechanism. A better understanding of this zone could lead to a better estimation of the pile tip bearing capacity because the size and position of this plastic zone are directly related to the pile tip bearing capacity. Therefore, this plastic zone has been studied for different soil and pile parameters. Also, the influence of each parameter has been studied and discussed. A similar balloon shaped plastic zone was found for both small and large displacement simulations.

The tip bearing capacity of a pile is regarded to depend only on the soil in a certain zone around the pile tip. This zone is called the influence zone. The influence zone is found to be similar to the plastic zone of a pile tip. Therefore, the influence of a soft soil layer, near the influence zone of the pile tip, has also been studied. The numerical results have been validated with laboratory tests made by Deltares. The influence zone is roughly from 2 times the pile diameter, *D*, above the pile tip, to 5 or 6 times *D* below the pile tip.

Laboratory tests, using the direct shear test machine, have been performed in order to define the difference between the soil-pile friction angle and the soil-cone friction angle. The tests were done for different surface roughnesses and for three different sand types. The results were compared with the roughness of the sleeve of the Cone Penetration Test (CPT) apparatus.

Based on the numerical simulations and the laboratory tests of Deltares, a new design method has been proposed for the estimation of the pile bearing capacity. This method has as main input value, the CPT results, therefore it is a CPT-based design method. The proposed method has been validated using pile field tests that were performed in Lelystad in the Netherlands.

During this research, several axial and lateral pile field tests were performed at the West Coast of Mexico. Their results have been reported and discussed in the appendices.

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First, I am very grateful to my supervisor Prof. Van Baars for the endless support. His helpful comments, advice and encouragement throughout the duration of my research were crucial in succeeding my dissertation.

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Shilton RICA

Luxembourg, September 2019

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List of Abbreviations and Symbols

Abbreviations		Definition
СРТ		Cone Penetration Test
CEM		Cavity Expantion Method
DEM		Discrete Element Method
FDM		Finite Difference Method
FEM		Finite Element Method
ICP		Imperial College Pile
IP		Installed Pile
		Laboratoire Central des Ponts et Chausées
LE, C		Lagrangian —Fulerian
		Material Point Method
		Manard Pressionater Test
MSI		Main Sea Level
		Main Sea Level
		Niguwa Europasa Norman (Dutch angingaring norms)
		Nerwagian gootochnical Instituto
		Pilolo-Eldslicity Destine Finite Floment Method
		Particle Finite Element Method
		Particle image velocimetry
PRI		Press-Replace Technique
РВР		Pre-Boring Pressiometers
SBP		Self-Boring Pressiometers
SPT		Standard Penetration Test
UWA		University of western Australia
WIP		Wished In Place
Px		Pixel (from PIV measurements)
Cte		constant
		constant
Latin Symbols	SI	Definition
Latin Symbols A _{si}	SI [m ²]	Definition The shaft area of the pile within the <i>i</i> -th soil layer
Latin Symbols A_{si} $A^a_{s,i}$	SI [m ²] [m ²]	Definition The shaft area of the pile within the <i>i</i> -th soil layer The shaft surface along the pile length above the neutral plane
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e_{min}	[-]	The minimum possible void ratio of the soil sample
e_{max}	[-]	The maximum possible void ratio of the soil sample
F_s	[kN]	The pile shaft friction
$F_{s,c}$	[kN]	The calculated pile shaft friction
$F_{s,m}$	[kN]	The measured pile shaft friction
F_t	[kN]	The pile tip bearing capacity
$\tilde{F}_{t,c}$	[kN]	The calculated pile tip bearing capacity
$F_{t,m}$	[kN]	The measured pile tip bearing capacity
$F_{tot c}$	[kN]	The total calculated pile bearing capacity
Ftot hoad	[kN]	The measured pile bearing capacity at the pile head
$F_{t,m(t)}$	[kN]	The measured pile tip bearing capacity t -time after installation
$F_{i,m(i)}$	[kN]	The measured nile tip bearing capacity directly after installation
$f_{t,m(t_0)}$		The friction number from CDT measurements
J f()	[-]	The represents a function of
ʃ () f f	[-]	Empirical boaring capacity factors
Jb, Js f /f	[-]	Empirical Dearing Capacity factors
Jt/Jc C		The cheer modulus of the soil
G II		The death of the ails tin in the sail (from the sail lovel)
П _{pile}		The depth of the plie up in the son (from the son level)
H _{ch}	[m]	The height of the chamber (laboratory tests)
n	[m]	The high above the pile tip
h _d	[m]	The penetration depth in end-bearing layer
h _{ws}	[m]	The thickness of the thin weak soil layer
K ₀	[-]	The coefficient of the lateral earth pressure coefficient
K _a	[-]	The active earth pressure coefficient
K_p	[-]	The passive earth pressure coefficient
k	[-]	The cavity parameter (for cylindrical or spherical cavity)
k _p	[-]	The limit pressure coefficient (pile installation method and the soil type)
L	[m]	The pile length, below the ground soil level.
L _c	[m]	The critical depth of pile tip
l_c	[m]	The length of the central cell (Menard test)
m	[-]	The operative flow number for the plasticity zone
N_q, N_c, N_γ	[-]	The surcharge, the cohesion and the self-weight bearing capacity factor
p	[MPa]	The limit pressure, Prandtl's wedge
p_{atm}	[MPa]	The atmospheric pressure
p_0	[MPa]	The natural pressure of the soil at rest
p_L	[MPa]	The limit cavity pressure, cavity expansion theories
p_l	[MPa]	The limit cavity pressure (Menard test)
$p_{l;i}$	[MPa]	The limit value of the <i>i</i> -th measurement of the pressiometer
$p_{l;avg}$	[MPa]	The average value of the limit pressure
p_{ref}	[MPa]	The reference stress (equal to 1 atmosphere = 0.1 MPa)
<i>p</i> ′	[MPa]	The effective mean stresses of the soil at the pile tip
q	[MPa]	The surcharge
q_c	[MPa]	The cone resistance (unit CPT tip bearing capacity)
q_t	[MPa]	The unit pile tip bearing capacity
$q_{t_{resid}}$	[MPa]	The residual unit pile tip bearing capacity (after pile installation)
$q_{t.0.1}$	[MPa]	The unit pile tip bearing capacity for a $10~\%~D$ displacement of pile head
<i>q_{c,weak}</i>	[MPa]	The cone resistance of the weak layer
$q_{c,hard}$	[MPa]	The cone resistance of the hard layer
$q_{c:ava}$	[MPa]	The average value of q_c values within an influence zone
q _{c·i·ava}	[MPa]	The average value of q_c values in area $i = (I, II, III)$, Koppeian method
<i>q</i> _t	[MPa]	The unit pile tip bearing capacity according to Menard method
$R_{\rm P}$	[m]	The radius of the hardly deformed soil around the nile (installation)
R _c	[m]	The radius of the cavity zone
<i>C</i>	· · · · 1	

R_p	[m]	The radius of the plastic zone
R _{inter}	[-]	The parameter of the friction coefficient for the soil-pile interface
r_0	[m]	The distance from the centre of the pile/cone tip
Sr	[-]	The degree of the soil saturation
S	[-]	The shape factor of the pile tip
S_q, S_c, S_γ	[-]	The surcharge, the cohesion, the self-weight shape factor of the pile tip
V_0	[m³]	The volume of the cell at rest condition (Menard test)
V_c	[m³]	The initial volume of the central cell (Menard test)
V_m	[m³]	The mean value of the volume of the cell (Menard test)
W	[kN]	The self-weight of the foundation pile
W	[m]	The pile head displacement/settlement
<i>z</i> _b	[m]	The depth of pile embedment into hard layer

Greek Symbols

α, β	[-]	Empirical parameters
α_t	[-]	The pile tip factor (depending on the pile, soil, installation method etc.)
α_s	[-]	The pile shaft factor (depending on the pile, soil, installation method etc.)
β_t	[-]	The pile tip factor accounting for the shape of the pile tip
Ysoil	[kN/m³]	The unit self-weight of the soil (in natural condition)
Ywater	[kN/m³]	The unit self-weight of the water
Υsat	[kN/m³]	The unit self-weight of the saturated soil
Ymin	[kN/m³]	The minimum possible unit self-weight of the soil
Ymax	[kN/m³]	The maximum possible unit self-weight of the soil
γ'	[kN/m³]	The effective self-weight of the soil
δ_{f}	[°]	The interface friction angle at failure
$\delta_{soil-cone}$	[°]	The friction angle between the soil and the CPT-cone shaft
$\delta_{soil-pile}$	[°]	The friction angle between the soil and the pile shaft
Z	[-]	The factor representing the pile installation effects
θ_c	[°]	The half of the apex angle of the cone (CPT)
ν	[-]	The Poisson's ratio
λ	[-]	The shear stress ratio, $\lambda= au/\sigma$, regarding the direct shear test
$\lambda_{c,i}$	[-]	The constant/residual shear stress ratio, regarding the direct shear test
μ	[-]	The coefficient depending on the radius of the plastic zone
π	[-]	The "pi" number, which is equal to 3.14159
σ_{v}^{\prime} , σ_{h}^{\prime}	[MPa]	The vertical and the horizontal initial effective stresses
$\Delta \sigma_{rd}$	[MPa]	The change in radial stress during loading
$ au_s$	[MPa]	The shaft friction
$ au_{s,i}$	[MPa]	The unit shaft friction of the <i>i</i> -th soil layer
$ au^a_{s,i}$	[MPa]	The residual unit shaft friction above the neutral plane
$ au^b_{s,i}$	[MPa]	The residual unit shaft friction below the neutral plane
$ au_{sf}$	[MPa]	The local shear stress at failure
τ_u or τ_{soil}	[MPa]	The shear strength of the soil
τ_{soil}^{max}	[MPa]	The maximum shear strength of the soil
$ au_s^{ ext{CPT}}$	[MPa]	The CPT-cone shaft friction
τ_{s,i_M}	[MPa]	The unit pile shaft resistance of the <i>i</i> -th soil layer according to Menard test
ρ_s	[kN/m³]	The density of the soil grains
ϕ	[°]	The friction angle of the soil
ϕ_{peak}	[°]	The residual friction angle of the soil
ϕ_{resid}	[°]	The residual friction angle of the soil
ϕ_T	[°]	The friction angle of the soil near the penetrometer tip
ϕ_{ws}	[°]	The friction angle of the thin weak soil layer
ψ	[°]	The dilatancy angle of the soil
ψ_T	[°]	The dilatancy angle of the soil near the penetrometer tip