

Smoothed Particle Hydrodynamics for Ductile Solids

Von der Fakultät Konstruktions-, Produktions- und
Fahrzeugtechnik der Universität Stuttgart
zur Erlangung der Würde eines Doktor-Ingenieurs (Dr.-Ing.)
genehmigte Abhandlung

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*To my family, Ferdi and all the PC gamers out there
(especially the ones from Baesweiler)*

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