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Algorithms and software for efficient biomolecular simulation

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MARKUS CHRISTEN
Dipl. Chem. ETH
born March 29, 1975
citizen of Bülach (ZH) and Wynau (BE), Switzerland

accepted on the recommendation of
Prof. Dr. Wilfred F. van Gunsteren, examiner
Prof. Dr. Andrew E. Torda and Prof. Dr. Matthias Troyer, co-examiners

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Für Bea

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Kurzfassung

In den letzten fünfzig Jahren entwickelte sich die klassische Molekülsimulation in ein leistungsstarkes Werkzeug zur Untersuchung von biomolekularen Vorgängen auf atomarer Ebene. Dies wurde ermöglicht durch eine kontinuierliche Entwicklung der Simulationsverfahren und Programme. Im ersten Kapitel wird eine kurze Einführung in die klassische Simulation gegeben, mit speziellem Augenmerk auf Techniken um den durchsuchten Konfigurationsraum auf relevante Bereiche einzuschränken und auf die Berechnung von freien Energien aus den Simulationen. Als nächstes wird die neueste Version des Groningen Molecular Simulation Programmes GROMOS 05 vorgestellt. In dieser Version enthält das Programmpaket zwei Varianten des eigentlichen Simulationsprogrammes: eine erweiterte Version von PROMD, der traditionellen Simulationsmaschine von GROMOS, welche immer noch in FORTRAN geschrieben ist und das neu erstellte MD05 in C++. Dieses versucht durch Benutzen objektorientierter und generischer Programmier Techniken die Modularität und Lesbarkeit des Programmes zu erhöhen. Alle Simulationsverfahren, welche in den weiteren Kapiteln vorgestellt werden, sind in MD05 integriert.

In *Kapitel 3* wird ein kurzer Überblick über Methoden, welche den Konfigurationsraum effizient durchsuchen, gegeben. Danach folgt ein genauerer Blick auf die Berechnung von Entropien im Zusammenhang mit Kopie - Austausch in stochastisch dynamischen Simulationen. Dies geschieht anhand eines einfachen Testsystems, bei welchem vollständige Abdeckung des Konfigurationsraumes in Simulationen bei höheren Temperaturen erreicht werden kann. Bei diesen Temperaturen sollten somit auch die berechneten Eigenschaften unabhängig von der Simulationsmethode sein und erwartungsgemäss erfüllte Kopie - Austausch Simulation diese Bedingung. Bei tiefen Temperaturen ist keine vollständige Abdeckung mehr möglich. Kopie - Austausch Simulation kann unter diesen Umständen effizienter als die standard Simulationsmethode sein. Entropien von Simulationen werden häufig aufgeteilt in Rotations-, Translations- und Konfigurationsentropien. Dies wird erreicht durch eine Rotationsüberlagerung der Strukturen vor der Berechnung. Es konnte gezeigt werden, dass gewisse Überlagerungstechniken die Rotationsentropie bei tiefen Temperaturen gegenüber der Konfigurationsentropie stark bevorzugen.

Ein Verfahren, um eine fein-körnige (atomistische) und eine grob-körnige Representation eines Systems zugleich zu simulieren wird in *Kapitel 5* gegeben. Der momentane Zustand kann

durch einen Körnigkeits Regler angegeben werden. Es ist möglich, die Körnigkeit während einer Simulation kontinuierlich von fein-körnig zu grob-körnig und zurück zu ändern, oder auch viele Kopien gleichzeitig bei unterschiedlicher Körnigkeit zu simulieren und durch Kopie - Austausch die fein-körnigen Kopien von dem schnelleren Absuchen des Konfigurationsraumes der grob-körnigen Kopien profitieren zu lassen.

Ein unterschiedlicher Ansatz, um die Effizienz von Simulationen zu steigern, wird in *Kapitel 6* aufgezeigt. Um eine freie Energie Differenz zwischen zwei Zuständen zu berechnen, muss die Simulation diese beiden Zustände verbinden. Damit dies schneller geschieht, kann man den Konfigurationsraum, welcher der Simulation zur Verfügung steht, einschränken. Wenn diese Zwänge so formuliert werden können, dass sie nichts zur potentiellen Energie und den Kräften in den Endzuständen beitragen, dann bleibt die berechnete freie Energie unabhängig von dem erzwungenen Pfad, der die Zustände verbindet. Diese Methode ist für Distanz- und Dihedralwinkelbeschränkungen ausgearbeitet und wird an der Ionen - Bindung eines zyklischen Peptides und an der Berechnung der freien Energie Differenz von zwei Zucker Konformationen gezeigt. Im zweiten Beispiel wird die Methode verglichen mit Resultaten erhalten aus einem Potential der mittleren Kraft.

Der Simulation auferlegte Zwänge können auch dazu benutzt werden, um experimentell bestimmte Eigenschaften zu reproduzieren. Eine Simulation kann von experimentellen Eigenschaften abweichen, wenn das verwendete Kraftfeld nicht für das Problem geeignet ist, oder wenn die Simulationszeit nicht ausreicht, um alle notwendigen Konfigurationen, die zum experimentellen Resultat beitragen, zu besuchen. Beide Probleme können durch geschickt gewählte Zwänge verkleinert werden. In *Kapitel 7* werden Zwänge vorgestellt, die sich während der Simulation anpassen. Dies wird durch eine Kombination mit der Technik der örtlichen Erhebung erreicht, in welcher die potentielle Energie während der Simulation für bestimmte Konfigurationen angehoben wird. Diese Kombination ergibt zwei Hauptsächliche Vorteile. Erstens ergibt sich durch die langsame Anpassung der potentiellen Energiefunktion eine minimale Beeinflussung der Simulation durch die zusätzlichen Zwänge. Und zweitens wird lokal effizienter nach einer Konfiguration gesucht, welche die experimentellen Eigenschaften wiedergibt.

In den zwei nächsten Kapiteln werden nicht mehr Zwänge angeschaut, sondern der Simulation Nebenbedingungen hinzugefügt, welche exakt erfüllt sein müssen. Diese Nebenbedingungen werden beispielsweise dazu gebraucht, um Bindungen starr zu machen. Es ist nun möglich, eine zusätzliche Flexibilität einzufügen, mit welcher die starren Bindungslängen sich in einem gewissen Mass an Veränderungen in der Umgebung anpassen können. Die Methode der flexiblen Nebenbedingungen wird angewendet in einer Simulation von Neopentan unter hohem Druck und in einer vergleichenden Studie von Modellen mit unterschiedlicher Behandlung von Bindungen.

Zum Schluss wird in *Kapitel 10* auf mögliche zukünftige Entwicklungen von Simulationsprogrammen und effizienten Algorithmen hingewiesen.

Summary

Over the last fifty years, continuous development of simulation algorithms and software has made classical molecular dynamics simulation into a powerful tool to investigate biomolecular processes in atomistic detail. After a short introduction of classical simulation with special attention to biased sampling of configurational space and some techniques to calculate free energies, the latest version of the Groningen Molecular Simulation package is introduced:

GROMOS05. In this version, the heart of the package is delivered in two variants. An enhanced version of PROMD, the FORTRAN simulation engine, and MD05, written in C++. MD05 strives for higher modularity and readability by making use of object oriented features and generic programming techniques. All algorithms presented in the other chapters are integrated into MD05.

A brief overview and classification of searching methods is given in *Chapter 3* before a closer look is taken at entropies calculated by replica-exchange stochastic dynamics simulations. For the simple test system complete sampling of configurational space can be achieved. Therefore the entropies calculated from standard stochastic dynamics simulations should match the ones obtained from the replica-exchange simulations. This was found to be true. At low temperature and incomplete sampling of the configurational space, replica-exchange simulation can be more efficient if the simulation parameters are carefully selected. The procedure of rotationally fitting structures to decompose entropy into configurational, translational and rotational entropies has a significant impact on this decomposition, often disfavouring configurational entropy at low temperatures.

An algorithm to combine fine-grained (atomistic) simulations with coarse-grained ones is introduced in *Chapter 5*. The algorithm allows to either continuously vary the grain-level of the simulation from fully fine-grained to coarse-grained and back, or, using replica exchange, simultaneously simulate a system at fine-grained, at coarse-grained and at some intermediate grain levels. The higher the grain level the bigger the simulation time-step may be, therefore increasing sampling efficiency. Through replica exchange, the replicas at lower grain-level can profit from the faster sampling available at the higher levels.

A different way to improve sampling is shown in the next chapter, where the simulation is restrained to follow a reaction coordinate from a given state *A* to a state *B* for obtaining the free energy difference between these two states. Opposed to standard methods, the restraining

functions are chosen to have zero potential energy and forces in the end states (*A* and *B*). This permits the calculation of a path independent free energy difference. The method, implemented in terms of distance and dihedral restraints is applied to ion-complexation in a cyclic peptide and the calculation of the relative stability of two different chair conformations of a glucopyranoside. For the second case a comparison with a potential of mean force calculated using dihedral-angle constraints is given.

Further on, restraints can be used to force a simulation to reproduce experimental data. If the force field is not well suited to represent a biomolecule or if the simulation time is not long enough to sample the relevant part of the configurational space, experimental properties might not be reproduced by simulations. Both problems may be overcome by adding restraints. In *Chapter 7* adaptive restraints based on local-elevation simulation are introduced. Adaptive restraints have two main advantages: First, as the restraint force slowly builds up over the simulation time, and only if the restraint is not fulfilled, a minimum of force is added, which leads to the least possible disturbance of the simulation. Second, as the adaptive restraint is based on local-elevation simulation, locally enhanced sampling is achieved, until the restraint is fulfilled.

In the next two chapters the focus is no longer on restraints but on constraints. But these are flexibilized using an approximate, but fast algorithm, which enables simulations to use a comparatively large time-step but still have the constraints slowly adapt to changes in the environment. Using this technique, fast bond vibrational frequencies can be avoided. The method is applied to neopentane simulations under high pressure and to a comparative study of different models of flexibility. In this study, the free energy difference of water and methanol is calculated by thermodynamic integration.

Finally, in *Chapter 10* an outlook of future development with regard to simulation software and configurational sampling is provided.

Publications

This thesis has led to the following publications:

Chapter 2:

Markus Christen, Philippe H. Hünenberger, Dirk Bakowies, Riccardo Baron, Roland Bürgi, Daan P. Geerke, Tim N. Heinz, Mika A. Kastenholz, Vincent Kräutler, Chris Oostenbrink, Christine Peter, Daniel Trzesniak, and Wilfred F. van Gunsteren,
“ The GROMOS Software for Biomolecular Simulation: GROMOS05 ”
J. Comput. Chem. **26** (2005), 1719–1751

Chapter 3:

Markus Christen and Wilfred F. van Gunsteren,
“ On searching in, sampling of, and dynamically moving through conformational space of biomolecular systems: a review ”
J. Comput. Chem. (2006), accepted

Chapter 5:

Markus Christen and Wilfred F. van Gunsteren,
“ Multigraining: an algorithm for simultaneous fine-grained and coarse-grained simulation of molecular systems ”
J. Chem. Phys. **124** (2006), 154106

Chapter 6:

Markus Christen, Anna-Pitschna E. Kunz, and Wilfred F. van Gunsteren,
“ Sampling rare events using hidden restraints ”
J. Phys. Chem. B **110** (2006), 8488–8498

Chapter 8:

Markus Christen and Wilfred F. van Gunsteren,

“ An approximate but fast method to impose flexible distance constraints in molecular dynamics simulations ”

J. Chem. Phys. **122** (2005), Art. No. 144106

Related publications:

Wilfred F. van Gunsteren, Dirk Bakowies, Roland Bürgi, Indira Chandrasekhar, Markus Christen, Xavier Daura, Peter Gee, Alice Glättli, Tomas Hansson, Chris Oostenbrink, Christine Peter, Jed Pitera, Lukas Schuler, Thereza Soares, and Haibo Yu,
“Molecular dynamics simulation of biomolecular systems”
CHIMIA **55** (2001), 856–860

Thereza A. Soares, Markus Christen, Kai F. Hu, and Wilfred F. van Gunsteren ,
“ Alpha- and beta-polypeptides show a different stability of helical secondary structure ”
Tetrahedron **60** (2004), 7775–7780

Wilfred F. van Gunsteren, Dirk Bakowies, Riccardo Baron, Indira Chandrasekhar, Markus Christen, Xavier Daura, Peter Gee, Daan P. Geerke, Alice Glättli, Philippe H. Hünenberger, Mika A. Kastenholz, Chris Oostenbrink, Merijn Schenk, Daniel Trzesniak, Nico F. A. van der Vegt, and Haibo B. Yu,
“ Biomolecular modelling: goals, problems perspectives ”
Angew. Chem. Int. Ed. **45** (2006), 4064–4092

Bettina Keller, Markus Christen, Chris Oostenbrink, and Wilfred F. van Gunsteren ,
“ On using oscillating time-dependent restraints in MD simulation ”
J. Biomol. NMR (2006), accepted