

A parametric turbulence closure
for simple gas phase chemistry
in an extended Eddy Break-Up
combustion model

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Peter P. Breithaupt

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— *for Monique, Daan and Douwe* —
— *and my parents* —

Berichte aus der Energietechnik

Peter P. Breithaupt

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Haren, The Netherlands, May 2001

Peter P. Breithaupt

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