Shayan Hassanpour

Source & Joint Source-Channel Coding Schemes Based on the Information Bottleneck Framework

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Prof. Dr.-Ing. Armin Dekorsy

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Preface

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Contents

Preface **III**

1 Introduction **1**
1.1 Motivation 1
1.2 Objective 2
1.3 Outline 3
1.4 Contributions 4
1.5 Nomenclature 7

2 Uniterminal IB-Based Noisy Source Coding **9**
2.1 Chapter Overview 9
2.2 System Model and Problem Statement 9
2.3 Algorithmic Approaches for Arbitrary Source Alphabet . . . 13
2.3.1 Iterative IB 14
2.3.2 Agglomerative IB 16
2.3.3 Sequential IB 17
2.3.4 Deterministic IB 18
2.3.5 KL-Means IB 19
2.3.6 Double-Maxima IB 22
2.3.7 Affinity Propagation IB 24
2.3.8 0-1 Integer Program IB 29
2.4 Algorithmic Approaches for Binary Source Alphabet 30
2.4.1 Optimal Solution Finder 30
2.4.2 Modified Agglomerative IB 31
2.4.3 Modified Sequential IB 32
2.5 Numerical Investigations 33
2.5.1 Iterative IB vs. Sequential IB 34
2.5.2 Evidence of Equivalence 34
2.5.3 Performance of Affinity Propagation IB 35
2.5.4 Performance of Modified Agglomerative IB 37

2.6 Proof of Equivalence . . . 39
2.7 Chapter Summary . . . 40

3 Multiterminal IB-Based Noisy Source Coding 43
3.1 Chapter Overview . . . 43
3.2 System Model and Problem Statement . . . 43
3.3 Algorithmic Approaches . . . 46
3.3.1 Double-Maxima MTIB . . . 47
3.3.2 Parallel IB . . . 49
3.3.3 Alternating IB . . . 59
3.3.4 Successive IB . . . 60
3.4 Numerical Investigations . . . 66
3.4.1 Joint vs. Separate Design . . . 67
3.4.2 Successive IB vs. Alternating IB . . . 68
3.4.3 Parallel vs. Successive Retrieval . . . 69
3.5 Proofs . . . 71
3.5.1 Proof of Theorem 3.1 . . . 71
3.5.2 Parallel IB Convergence . . . 73
3.5.3 Successive IB Convergence . . . 75
3.6 Chapter Summary . . . 77

4 Uniterminal IB-Based Joint Source-Channel Coding 79
4.1 Chapter Overview . . . 79
4.2 System Model and Problem Statement . . . 79
4.3 Algorithmic Approaches . . . 81
4.3.1 Forward-Aware Double-Maxima IB . . . 82
4.3.2 Forward-Aware Affinity Propagation IB . . . 83
4.3.3 Forward-Aware 0-1 Integer Program IB . . . 85
4.3.4 Channel-Optimized Impurity IB . . . 85
4.3.5 MI-Based Channel-Optimized (Vector) IB . . . 87
4.3.6 Forward-Aware (Vector) IB . . . 88
4.4 Numerical Investigations . . . 93
4.4.1 A Square Symmetric Forward Model . . . 94
4.4.2 A Non-Square Forward Model . . . 100
4.4.3 A Square BSC-Based Bit-Pipe Forward Model . . . 101
4.4.4 A Mixed Forward Model . . . 107
4.5 Proofs . . . 109
4.5.1 Proof of Equivalence . . . 110
4.5.2 Proof of Theorem 4.1 . . . 112
4.5.3 Proof of Theorem 4.2 . . . 113
4.6 Chapter Summary . . . 113

5 Multiterminal IB-Based Joint Source-Channel Coding 115
5.1 Chapter Overview . . . 115
5.2 System Model and Problem Statement . . . 115
5.3 Algorithmic Approaches . . . 118
5.3.1 Forward-Aware Double-Maxima MTIB . . . 118
5.3.2 Forward-Aware Parallel IB . . . 120
5.3.3 Forward-Aware Successive IB . . . 123
5.4 Numerical Investigations . . . 128
5.4.1 (Forward-) Awareness vs. Unawareness . . . 128
5.4.2 Joint vs. Separate Design . . . 131
5.4.3 Parallel vs. Successive Retrieval . . . 132
5.5 Proofs . . . 134
5.5.1 Proof of Theorem 5.1 . . . 134
5.5.2 Forward-Aware Parallel IB Convergence . . . 136
5.5.3 Proof of Theorem 5.2 . . . 137
5.5.4 Forward-Aware Successive IB Convergence . . . 139
5.6 Chapter Summary . . . 141

6 Summary 143

A Information Theory Basics 147
A.1 Shannon's Entropy . . . 147
A.2 Conditional Entropy . . . 147
A.3 KL Divergence . . . 148
A.4 JS Divergence . . . 149
A.5 Mutual Information . . . 149
A.6 Conditional Mutual Information . . . 149
A.7 Chain Rule for Mutual Information . . . 150
A.8 Data Processing Inequality . . . 150

B Constrained Optimization 151
B.1 Method of Lagrange Multipliers . . . 151
B.2 Functional Derivatives . . . 153

C Affinity Propagation 155
C.1 K-Medoids Objective Function Extension . . . 155
C.2 Efficient Search via Belief Propagation . . . 156

D Multivariate IB 159
D.1 Multivariate Agglomerative IB . . . 159
D.2 Multivariate Sequential IB . . . 160

Abbreviations **161**

List of Symbols **163**

Bibliography **169**

Index **181**