

Institut für Landwirtschaftliche Betriebslehre der Universität Hohenheim  
Fachgebiet Produktionstheorie und Ressourcenökonomik im Agrarbereich  
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# **Calibrating Regional Production Models Using Positive Mathematical Programming**

An Agro-environmental Policy Analysis in Southwest Germany

Dissertation zur Erlangung des Grades eines Doktors der  
Agrarwissenschaften der Fakultät IV – Agrarwissenschaften II

von

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aus Mainz

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**Johannes Umstätter**

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## List of abbreviations and units

AC.....	average costs
AGM.....	average gross margin
AR.....	average revenue
AY.....	average yield
CAP.....	Common Agricultural Policy
DM.....	Deutsche Mark
dt.....	decimal ton
EU.....	European Union
ha.....	hectare
kg.....	kilogram
km.....	kilometer
l.....	liter
LP.....	Linear Programming
LSU.....	livestock units
MC.....	marginal costs
MEKA.....	Marktentlastungs- und Kulturlandschaftsausgleich
mg.....	milligram
MGM.....	marginal gross margin
Mill.....	million
MR.....	marginal revenue
MRS.....	marginal rate of substitution
MY.....	marginal yield
NLP.....	Nonlinear Programming
PMP.....	Positive Mathematical Programming
t.....	metric ton
TC.....	total costs
TGM.....	total gross margin
TR.....	total revenue
VMP.....	value marginal product