Ban-Sok Shin

Signal Processing for Distributed Kernel-based Estimation

Band 9

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Prof. Dr.-Ing. Armin Dekorsy

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Preface

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